PAPER • OPEN ACCESS

Opto-electronic properties and solar cell efficiency modelling of Cu_2ZnXS_4 (X = Sn, Ge, Si) kesterites

To cite this article: Thomas Ratz et al 2021 J. Phys. Energy 3 035005

View the article online for updates and enhancements.

You may also like

- <u>Vapor Phase Epitaxial Growth of ZnSiAs₂</u> on Ge and GaAs Substrates
 J. E. Andrews, H. H. Stadelmaier, M. A. Littlejohn et al.
- <u>Spectral characteristics of</u> <u>Sr₂ZnSi₂O₇:Eu²⁺,Dy³⁺/PAN spectrum-</u> <u>fingerprint anti-counterfeiting fiber</u> Jishu Zhang, Yingzi Zhang, Jin Tao et al.
- The pressure-effects on phase transitions, band structures, electronic and elastic properties of ternary compounds ZnXP₂ (X = Si, Ge, Sn) by first principle calculations
 Hui Liu, Beijun Zhao, You Yu et al.

This content was downloaded from IP address 146.103.254.11 on 23/02/2022 at 09:54

Journal of Physics: Energy

CrossMark

OPEN ACCESS

RECEIVED 22 December 2020

REVISED

11 March 2021

ACCEPTED FOR PUBLICATION 17 March 2021

PUBLISHED 30 June 2021

Original Content from this work may be used under the terms of the Creative Commons Attribution 4.0 licence.

Any further distribution of this work must maintain attribution to the author(s) and the title of the work, journal citation and DOI.



Opto-electronic properties and solar cell efficiency modelling of Cu_2ZnXS_4 (X = Sn, Ge, Si) kesterites

Thomas Ratz^{1,2,*}, Jean-Yves Raty^{1,3}, Guy Brammertz⁴, Bart Vermang^{2,4,5} and Ngoc Duy Nguyen¹

¹ CESAM, Q-MAT, Solid State Physics, Interfaces and Nanostructures, Physics Institute B5a, Allée du Six Août 19, B-4000 Liège, Belgium
² Institute for Material Baccarek (IMO), Haccalt University, Anorelean ack ways II, B, 2500 Diamethack, Belgium

- Institute for Material Research (IMO), Hasselt University, Agoralaan gebouw H, B-3590 Diepenbeek, Belgium
- ³ University of Grenoble Alpes, CEA-LETI, MINATEC Campus, Rue des Martyrs 17, F-38054 Cedex 9 Grenobles, France
 - IMEC division IMOMEC, partner in Solliance, Wetenschapspark 1, B-3590 Diepenbeek, Belgium
- Energyville, Thor Park 8320, B-3600 Genk, Belgium
- Author to whom any correspondence should be addressed.

E-mail: thomas.ratz@uliege.be

Keywords: kesterite, S compounds, first-principles calculations, Sn cation substitution, opto-electronic, efficiency modelling Supplementary material for this article is available online

Abstract

5

PAPER

In this work, first-principles calculations of Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂ZnSiS₄ are performed to highlight the impact of the cationic substitution on the structural, electronic and optical properties of kesterite compounds. Direct bandgaps are reported with values of 1.32, 1.89 and 3.06 eV respectively for Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂ZnSiS₄ and absorption coefficients of the order of 10⁴ cm⁻¹ are obtained, indicating the applicability of these materials as absorber layer for solar cell applications. In the second part of this study, ab initio results are used as input data to model the electrical power conversion efficiency of kesterite-based solar cells. In that perspective, we used an improved version of the Shockley–Queisser model including non-radiative recombination via an external parameter defined as the internal quantum efficiency. Based on predicted optimal absorber layer thicknesses, the variation of the solar cell maximal efficiency is studied as a function of the non-radiative recombination rate. Maximal efficiencies of 25.71%, 19.85% and 3.10% are reported respectively for Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂ZnSiS₄ for vanishing non-radiative recombination rate. Using an internal quantum efficiency value providing experimentally comparable $V_{\rm OC}$ values, cell efficiencies of 15.88%, 14.98% and 2.66% are reported respectively for Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂ZnSiS₄. We confirm the suitability of Cu₂ZnSnS₄ in single junction solar cells, with a possible efficiency improvement of nearly 10% enabled through the reduction of the non-radiative recombination rate. In addition, Cu₂ZnGeS₄ appears to be an interesting candidate as top cell absorber layer for tandem approaches whereas Cu_2ZnSiS_4 might be interesting for transparent photovoltaic windows.

1. Introduction

Over the years, photovoltaic (PV) thin film technology has emerged as an interesting candidate for efficient and large-scale energy production. To this aim, this technology must fulfill several criteria such as low-cost thin film synthesis, high solar cell efficiency and the materials' resources availability and accessibility [1]. In relation to the latter point, the European Commission has identified Ga and In as critical raw materials and highlighted the scarcity of those elements used for the synthesis of inorganic chalcogenide CuInGa(S, Se)₂ (CIGS) alloys implemented as absorber layer for PV applications [2]. Despite the high efficiency reported for CIGS solar cells, with a record value of 23.3% [3, 4], the incorporation of this material in a large-scale energy production technology might be compromised. This justifies an urgent search for alternative compositions with comparable or better efficiencies than CIGS. As a consequence, over the past 20 years, the scientific community has been investigating kesterite $Cu_2ZnSn(S, Se)_4$ materials as an absorber layer in solar cell applications [5]. Benefiting from the well-established knowledge of CIGS, kesterite-based solar cell efficiency gradually increased over the years, reaching values of 12.6% for $Cu_2ZnSn(S, Se)_4$ [6] and 11% for Cu_2ZnSnS_4 [7] using various chemical [8] or physical [9] routes for the synthesis of the kesterite thin films.

However, new challenges concerning further efficiency improvements have recently arisen. Large open circuit voltage V_{OC} deficits have been reported as responsible for the efficiency limitation encountered [5, 10]. Several elements have been pointed out as possible culprits for the V_{OC} deficits, including interface recombination due to band misalignment [11, 12], formation of secondary phases, and/or high intrinsic point defect concentration leading to non-radiative recombination in the kesterite bulk material [13, 14]. As a result, recombination centres are present both at the architectural level (band misalignment with the buffer layer) and at the compositional/morphological level (defects and/or secondary phases) within the absorber layer. Focusing on the kesterite absorber layer, several solution paths have been considered to overcome the current efficiency limitation, like alloying using isoelectronic substitution elements such as Ag for Cu, Ge for Sn or Se for S [15, 16] or via the cationic substitution of Zn or Sn [17, 18].

In the past, alternative kesterite materials have been studied both theoretically and experimentally, leading to promising efficiencies for Ge-containing kesterite compounds [19–24]. Using density functional theory (DFT) calculations, a few works reported predictions over structural properties, electrical properties or optical properties of alternative kesterite materials such as Cu_2ZnSnS_4 [25–31], Cu_2ZnGeS_4 [25–27, 32, 33] and Cu_2ZnSiS_4 [25–27]. However, the variety of computational approaches do not facilitate the comparison of the materials' physical properties. In addition, to the best of our knowledge, the DFT results are rarely compared to experimental measurements.

In this work, we first investigate theoretically the cationic substitution of Sn by two other isoelectronic elements: Ge and Si, in kesterite Cu_2ZnSnS_4 . The structural and opto-electronic properties are calculated for Cu_2ZnSnS_4 as the reference material [9], Cu_2ZnGeS_4 as a promising material regarding the experimental efficiency achieved [9, 23] and Cu_2ZnSiS_4 as an interesting candidate regarding the elemental abundance [1]. Then, the obtained *ab initio* results are used as input data to feed an improved version of the Shockley–Queisser model [34], allowing us to connect the intrinsic material properties to the solar cell macroscopic properties. Via this cell efficiency modelling, physical quantities such as the open circuit voltage V_{OC} , the short circuit current density J_{SC} and the fill factor *FF* are computed.

In the first section of this paper, the structural properties of the materials are presented. Then, in the following sections, the Heyd–Scuseria–Ernzerhof exchange-correlation functional (HSE06) [35] is used to compute the electronic and optical properties. Based on the band structures and the densities of states (DOS), the electrical properties of the materials are reported and compared. To complete the investigation, the optical properties are presented and related to the electrical properties. This approach allows us to extract the general trends highlighting the impact of the cationic substitution of Sn by Ge and Si on the opto-electronic properties. In the second part of this work, using the *ab initio* results as input data, the upper limit of the kesterite-based solar cell efficiency is calculated using the theoretical model proposed by Blank *et al* [36]. This model allows us to compute physical quantities that can be compared to experimental results such as the solar cell efficiency η .

2. Computational method

First-principles calculations have been performed using Vienna *ab initio* simulation package code [37] with the projector-augmented wave potential method [38]. Perdew–Burke–Ernzerhof GGA pseudo-potentials [39] were used with the following valence electrons considered for each element: Cu: $3d^{10}4s^1$, Zn: $3d^{10}4s^2$, Sn: 4d¹⁰5 s²5p², Ge: 3d¹⁰4 s²4p², Si: 3 s²3p² and S: 3 s²3p⁴. Ionic and electronic relaxations were achieved using a cut-off energy of 550 eV and a Γ -centred uniform **k**-points mesh of $6 \times 6 \times 6$ **k**-points. Applying the strongly constrained and appropriately normed semilocal density functional (SCAN) [40, 41], the structures were relaxed until the numerical convergence regarding the self-consistent cycles reaches forces between ions less than 10^{-3} eV Å⁻¹. The system total energy was converged down to 10^{-6} eV. During the relaxation, the symmetry was kept constant to the kesterite point group symmetry (I - 4) and the atomic positions, cell volume and cell shape were allowed to relax. The SCAN meta-GGA functional was proven effective to predict improved geometries for a computational cost comparable to the GGA functional. Moreover, Fritsch et al reported that the combination of SCAN functional calculations for ionic relaxations followed by a single HSE06 functional electronic calculation provides accurate results for kesterite materials [42]. Consequently, starting from the relaxed structure, the HSE06 exchange-correlation functional, known for its bandgap prediction accuracy [43], was used to compute the electronic and optical properties. Concerning the optical calculations, the imaginary part of the dielectric tensor was first obtained via a sum over states by applying the Fermi golden rule between valence band and conduction band states at a given k-point. Then, the real

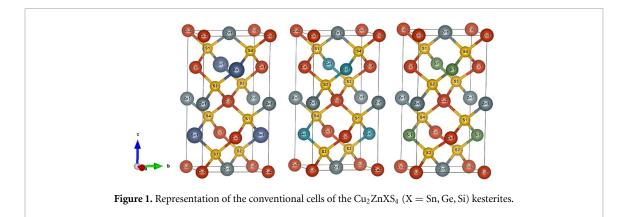


Table 1. Lattice parameters *a*, *b* and *c* (see figure 1) and conventional cell volume *V* of Cu_2ZnXS_4 (X = Sn, Ge, Si) kesterites. Interatomic distances between the cation (X = Sn, Ge, Si) and the sulphur atom d_{X-S} are reported as well as the copper-sulphur distances d_{Cu-S} . Empty cells denote the absence of available data.

Materials	Reference (Type)	a, b (Å)	c (Å)	V (Å ³)	d_{X-S} (Å)	$d_{\mathrm{Cu-S}}$ (Å)
Cu ₂ ZnSnS ₄	This work	5.40	10.79	314.90	2.44	2.29
	[44] (Exp.)	5.67	11.30			
	[45] (Exp.)	5.42	10.79		2.39	2.33
	[46] (Exp.)	5.42	10.79			
	[47] (Exp.)	5.43	10.86			
	[48] (Exp.)	5.43	10.86			
	[49] (Exp.)	5.42	10.86			
	[26] (Theo.)	5.44	10.76			
	[28] (Theo.)	5.33	10.66			
	[29] (Theo.)	5.47	10.92			
	[27] (Theo.)	5.45				
	[30] (Theo.)	5.43	10.86			
	[31] (Theo.)	5.45	10.89			
Cu ₂ ZnGeS ₄	This work	5.30	10.51	294.87	2.26	2.28
	[47] (Exp.)	5.34	10.57			
	[49] (Exp.)	5.28	10.71			
	[50] (Exp.)	5.33-5.34	10.52-10.59	299.54-301.95		
	[51] (Exp.)	5.30-5.37	10.49-10.69			
	[26] (Theo.)	5.28	10.49			
	[27] (Theo.)	5.35				
	[32] (Theo.)	5.35	10.49			
	[33] (Theo.)	5.38	10.49			
Cu ₂ ZnSiS ₄	This work	5.25	10.32	283.94	2.15	2.28
	[26] (Theo.)	5.22	10.30			
	[27] (Theo.)	5.31				

part of the dielectric tensor was obtained thanks to a Kramers–Kroning transformation for which the convergence was properly ensured via a sufficiently high number of conduction band energy levels included in the calculation.

3. Results and discussion

3.1. Structural properties

The lattice parameters *a*, *b*, *c* (cf. figure 1), the conventional cell volume *V* and the atomic distances d_{Cu-S} and d_{X-S} (X = Sn, Ge, Si) were obtained as a result of the ionic relaxation (see table 1).

The sequential substitution of Sn by Ge and Si induces a contraction of the kesterite lattice parameters. A reduction of *a* and *b* from 5.40 Å (Cu₂ZnSnS₄) to 5.25 Å (Cu₂ZnSiS₄) is observed while the *c* parameter is reduced from 10.79 to 10.32 Å. The results reported in table 1 are in good agreement with experimental measurements for Cu₂ZnSnS₄ [44–49] and Cu₂ZnGeS₄ [47, 49–51]. To our knowledge, experimental characterisation of Si-pure kesterite crystal structures has not been reported yet. According to [52, 53], an orthorhombic crystalline structure is observed for high Si concentrations. Nevertheless, several theoretical works [26, 27] reported values close to *a*, *b* = 5.25 Å and *c* = 10.32 Å as obtained here. This lattice contraction can be interpreted by taking into account the successive reduction of the atomic radius of the substitutional

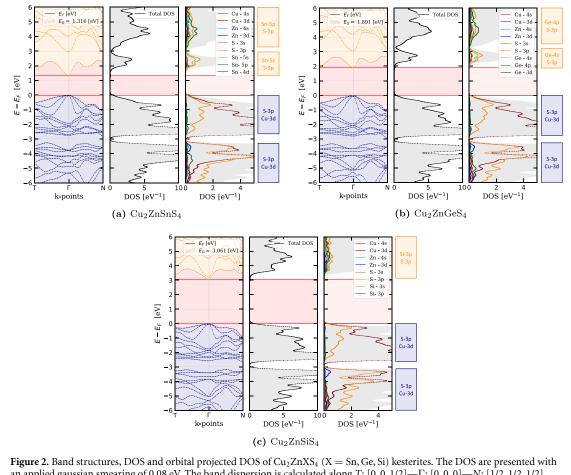


Figure 2. Band structures, DOS and orbital projected DOS of Cu_2ZnXS_4 (X = Sn, Ge, Si) kesterites. The DOS are presented with an applied gaussian smearing of 0.08 eV. The band dispersion is calculated along T: [0, 0, 1/2]— Γ : [0, 0, 0]—N: [1/2, 1/2, 1/2]. Main atomic orbital contributions to the DOS are presented alongside the figures.

cation from $r_{\text{Sn}} = 1.45$ Å, to $r_{\text{Ge}} = 1.25$ Å and to $r_{\text{Si}} = 1.10$ Å [54]. Consequently, the conventional cell volume decreases from 314.9 Å³ for the Sn-containing compound to 294.87 Å³ for Cu₂ZnGeS₄ and to 283.94 Å³ for Cu₂ZnSiS₄. One can also notice that the cation substitution does not impact the $d_{\text{Cu-S}}$ distances. In the following section, the results presented here will be put into perspective with the electronic properties.

3.2. Electronic properties

As it can be observed in figure 2, all calculated kesterite bands present a direct bandgap located at the Γ point. Using an approach similar to that reported in [25–27], the bandgap values reported in table 2 were obtained from the energy differences between the conduction band minimum and the valence band maximum energy levels as extracted from the Kohn–Sham eigenvalues. As reported in table 2, the bandgap energy E_G increases from 1.32 eV for Cu₂ZnSnS₄ to 1.89 eV for Cu₂ZnGeS₄ and to 3.06 eV for Cu₂ZnSiS₄. These results are comparable to those reported by Zamulko *et al* in their theoretical investigation [26]. In comparison to experimental values, the Sn-containing kesterite bandgap is underestimated by 0.18 eV as usual reported values are around 1.5 eV [9]. In contrast, the Cu₂ZnGeS₄ bandgap value of 1.89 eV fits with the reported experimental bandgaps with values between 1.88 and 2.25 eV [49–51, 55–57]. According to [58], a bandgap value of 2.71 eV was experimentally obtained for Cu₂ZnSiS₄.

We provide here a focus on the orbitals' projected DOS and their contributions to electronic states in the band structure, for the Sn-kesterite compound (figure 2(a)). The main contributions to the conduction band states come from S 3p and Sn 5s atomic orbitals close to the bottom of the band and S 3p and Sn 5p atomic orbitals for higher energy levels. Concerning the valence band, the hybridisation between Cu 3d and S 3p orbitals provide the main contributions to energy states at the top of the band. These results are corroborated by the work of Paeir *et al* in [31]. This tendency is also observed for the two other kesterite materials, i.e. the bottom of the cation Si and the 3p orbital of the chalcogen S, while the contributions to the top of the valence band come from the 3d atomic orbital of Cu and the 3p atomic orbital of the sulphur element.

Table 2. Bandgaps E_G and effective masses m^* scaled by the free electron mass m_0 of Cu₂ZnXS₄ (X = Sn, Ge, Si) kesterites. Effective masses have been calculated around the Γ high symmetry **k**-point and along two directions in the reciprocal space: [0,0,0] to [0,0,1] (resp. [0,0,0] to [0,1,0]) for the first effective mass component m_{\perp} (resp. for the second component $m_{//}$) comparable to values reported in [27]. High-frequency dielectric constants ϵ_{∞} of the materials are also presented and scaled with the vacuum electrical permittivity ϵ_0 comparable to values reported in [26].

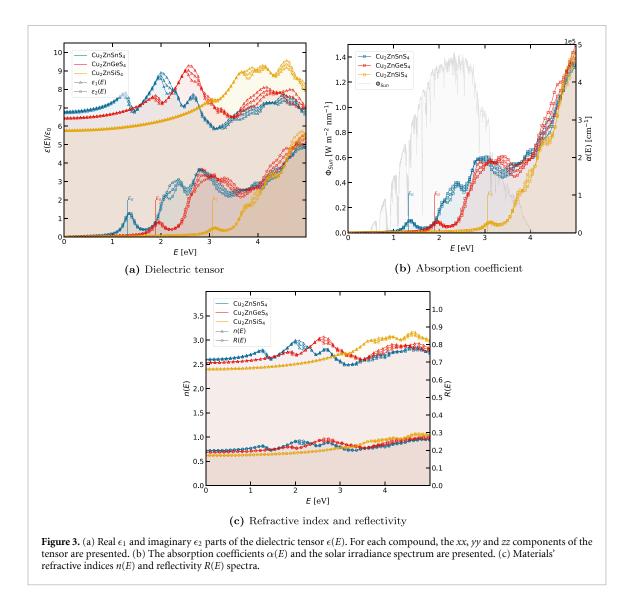
		$m_{//}^{*} [m_{e}]$				m_{\perp}^{*} $[m_{e}]$				
Materials	E_G (eV)	$\Gamma_{\nu,1}$	$\Gamma_{\nu,2}$	Γ _{ν,3}	Γ_c	Γ _{ν,1}	$\Gamma_{\nu,2}$	Γ _{ν,3}	Γ_c	$\epsilon_{\infty} \left[\epsilon_0 ight]$
Cu ₂ ZnSnS ₄	1.32 (This work) 1.50 [9] (Exp.) 1.26–1.77 [25, 26, 30, 31] (Theo.)	-0.69	-3.32	-0.16	0.19	-0.77	-0.64	-0.19	0.18	6.77
Cu ₂ ZnGeS ₄	1.89 (This work) 1.88–2.25 [49–51, 55–57] (Exp.) 2.10–2.38 [25, 26, 30, 32] (Theo.)	-0.72	-3.49	-0.19	0.23	-0.72	-0.63	-0.24	0.22	6.44
Cu ₂ ZnSiS ₄	3.06 (This work) 2.71 [58] (Exp.) 3.05 [25, 26] (Theo.)	-1.44	-3.65	-0.25	0.26	-1.63	-0.68	-0.33	0.25	5.78

For Cu₂ZnGeS₄ and Cu₂ZnSiS₄, the substitution of Sn by Ge and Si (figures 2(b) and (c)) seems to slightly flatten the energy level at the bottom of the conduction band. The bandgap increase from 1.32 to 3.06 eV is due to the variation of the chemical interaction between the cation and the sulphur, which leads to (i) a weak flattening of the energy level at the bottom of the conduction band and (ii) a shift of this energy level towards higher energies. To link those observations to the structural properties of the materials one can put into perspective the decrease of the cation/sulphur interatomic distance d_{X-S} with the increase of the kesterite bandgap. In contrast, the substitution of the cation atoms leaves the valence band unchanged as the orbitals contributing to these states are from Cu and S for which the interatomic distances d_{Cu-S} are reported constant from one kesterite material to another (cf. table 1).

In addition to the bandgaps, the effective masses are presented in table 2. These ones have been calculated around the Γ point, at the direct bandgap location, and along two directions in the reciprocal space: [0,0,0] to [0, 0, 1] for the first effective mass component m_{\perp} and along [0, 0, 0] to [0, 1, 0] for the second component m_{ll} . As shown in figure 2, one energy level is present at the bottom of the conduction band and three energy levels are located at the top of the valence band. Consequently, the effective masses have been calculated for the lowest energy level in the conduction band named Γ_c and for the three highest energy levels at the top of the valence band $\Gamma_{\nu,1}, \Gamma_{\nu,2}, \Gamma_{\nu,3}$, labeled from the highest energy level to the lowest energy level. For both the conduction and valence band, the general trend observed is a slight increase of the effective mass absolute value, with only two occasions of exceptions (for $\Gamma_{\nu,1}$ and $\Gamma_{\nu,2}$ of the m_1^* component), when Sn is sequentially substituted by Ge and Si. Then, as kesterite materials behave electrically as p-type semiconductor [10], we first discuss the hole effective mass values. As presented in table 2, concerning the $m_{1/2}^*$ component, $\Gamma_{\nu,2}$ effective masses are significantly higher than $\Gamma_{\nu,1}$ and $\Gamma_{\nu,3}$, highlighting the presence of light and heavy holes in this particular direction. In addition, similar values are reported regarding $\Gamma_{\nu,1}$ and $\Gamma_{\nu,3}$ for the perpendicular component while, in contrast, $\Gamma_{\nu,2}$ is five times lower than in the parallel direction. Concerning the electron effective masses, similar values are obtained for both components $m_{1/2}^*$ and m_1^* with a slight increase from a minimal value of 0.18 m_e to a maximal value of 0.26 m_e observed as the Sn cation is substituted. These values are in good agreement with those obtained by Liu et al with reported effective masses of 0.18, 0.21 and 0.26 m_e (resp. 0.19, 0.22, 0.24 m_e) in the parallel (resp. perpendicular) direction [27]. This suggests that the hole and electron effective masses would only slightly increase as Sn is substituted by Ge and then Si. In summary, the cationic substitution does not impact significantly the hole nor electron effective masses but leads to a significant increase of the kesterite bandgap.

3.3. Optical properties

Following the computation of the electronic properties, the optical properties of the kesterite materials have been determined via the calculation of the dielectric tensor $\epsilon(E)$ whose real ϵ_1 and imaginary ϵ_2 parts are shown in figure 3(a) (see supplementary material for the detailed equations (available online at stacks.iop.org/JPENERGY/3/035005/mmedia)). In this figure, the components *xx*, *yy* and *zz* of $\epsilon(E)$ are presented for each compound. It appears that the sequential substitution of Sn with Ge and Si leads to a decrease of the high frequency dielectric response ϵ_{∞} from 6.77 ϵ_0 (Cu₂ZnSnS₄) to 6.44 ϵ_0 (Cu₂ZnGeS₄) and reaching 5.78 ϵ_0 for the Si-containing compound (cf. table 2). These results are comparable to the values of 6.7 (Cu₂ZnSnS₄), 6.6 (Cu₂ZnGeS₄) and 5.7 (Cu₂ZnSiS₄) reported by Zamulko *et al* [26]. As expected, the decrease in ϵ_{∞} is in agreement with the increase of the materials' bandgap. Concerning the imaginary part of the dielectric tensor $\epsilon_2(E)$, the onset of absorption is also shifted towards higher energies as the bandgap



increases. In addition, in figure 3(a), one can notice that the peaks positions correspond well to the bandgaps reported in table 2.

Then, the absorption coefficient $\alpha(E)$ as well as the reflectivity R(E) and refractive index n(E) are computed as described in the supplementary material. In figure 3(b) the absorption coefficient of the materials are presented alongside the solar irradiance spectrum. First, one can notice that the kesterite compounds exhibit absorption coefficient values between 0 and 2×10^5 cm⁻¹ within the energy range of non-negligible solar irradiance (between 0.5 and 4 eV). This result highlights the applicability of these kesterite materials as the absorber layer in solar cell applications. However, an energetic shift of the absorption curves is also observed from the Sn-containing kesterite to the Si-containing kesterite with a first absorption peak located at the respective bandgap energies of the materials. The Cu₂ZnSnS₄ and Cu₂ZnGeS₄ curves have a similar behaviour while for the Si-containing kesterite curve, the plateau observed for the two other kesterites disappears as a consequence of the energy level shift at the bottom of the conduction (cf. figure 2(c)). Finally, in figure 3(c), the refractive index n(E) and reflectivity R(E) are presented. As reported, the refractive indices at 0 eV are 2.59, 2.53 and 2.40 respectively for Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂ZnSiS₄ with variations of 0.6 in values between 0 and 5 eV. Concerning the reflectivity values, a variation from 20% to 30% within the 0 to 5 eV energy range is observed. Additionally, it is worth noticing some reflectivity differences of nearly 10% between Cu₂ZnSnS₄ and Cu₂ZnSiS₄ for some energy values.

3.4. Electrical power conversion efficiency

In this section, we focus on the theoretical modelling of solar cell macroscopic physical quantities such as the short circuit current density J_{SC} , the open circuit voltage V_{OC} and the solar cell electrical power conversion efficiency η using Cu₂ZnXS₄ (X = Sn, Ge, Si) as the absorber layer. The predictions are realised based on the theoretical model presented by Blank *et al* [36]. The improvements proposed by Blank *et al* over the

Shockley–Queisser model [34] are (i) the use of the internal quantum efficiency Q_i as a model parameter to take into account non-radiative recombinations and (ii) the incorporation of light trapping by taking into account the refractive index n(E) in the calculation of the radiative current density $J_{rad,0}(n,d)$ (see supplementary material).

Non-radiative recombination occurs via recombination centres: intrinsic point defects, defect clusters and grain boundaries in the bulk materials or also through recombination centres at the interfaces of the various layers composing the solar cell. As a consequence, these recombination centres have an impact on the solar cell properties. Therefore, in this theoretical work, we chose to use the non-radiative recombination rate as a model parameter. In that perspective, the internal quantum efficiency is expressed as the ratio between the radiative recombination rate $R_{rad,0}$ and the total recombination rate: $R_{rad,0} + R_{nrad,0}$, leading to a non-radiative recombination rate under equilibrium conditions,

$$R_{\rm nrad,\,0} = R_{\rm rad,\,0} \frac{(1-Q_i)}{Q_i}.$$
(1)

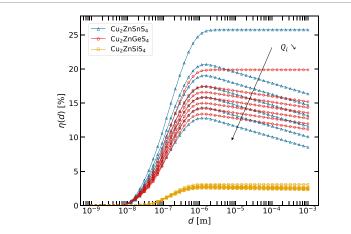
Considering a perfectly crystalline material, all recombinations are radiative and the photons emitted (i.e. not reabsorbed) contribute to the emission spectrum of the material which, in this model, is assumed as the black body spectrum at temperature T = 300 K. These radiative recombinations are therefore thermodynamically required and are proportional to the amount of electrons within the conduction band (i.e. proportional to the temperature). This first situation corresponds to an internal luminescence quantum efficiency Q_i value equals to unity for which the total recombination rate R_0 is equal to the radiative recombination rate Rrad, 0. In the case of recombination centres within the bulk materials or at the interfaces, both radiative and non-radiative recombination are included. The thermodynamic condition of emission must still be fulfilled ($R_{rad,0}$) and additionally, recombinations via recombination centres occur ($R_{rrad,0}$), leading to an increase of the total recombination rate R_0 . In this paper, the Q_i value is related to the amount of non-radiative recombinations which is proportional to the number of radiative recombinations (equation (1)). Q_i can consequently be related to the internal quantum efficiency IQE which is an experimentally measured physical quantity. The detailed description of the theoretical model proposed by Blank et al is presented in the supplementary material. To feed this theoretical model we use the previously calculated optical results ($\alpha(E)$, n(E) and R(E)) as input data. It is worth noticing that the computed material properties obtained correspond to a perfect crystal situation (i.e. $Q_i = 1$). As the internal quantum efficiency tends to vanish, variations of the optical properties are expected as defects will introduce new electronic states. However, in this work the perfect crystal optical properties are considered for each value of Q_i . Accordingly, the absorptance A(E) of the absorber layer is determined via equation (2), assuming a flat solar cell surface and a thin film thickness d:

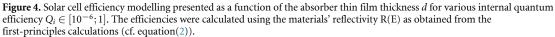
$$A(E,d) = [1 - R(E)] - \exp(-2\alpha(E)d).$$
(2)

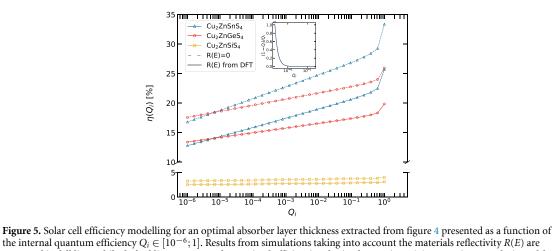
The obtained results are presented for a solar cell temperature T = 300 K as follows.

- First, we evaluate the optimal thicknesses (i.e. associated to a maximum for η) of the absorber layer as a function of Q_i . To this perspective, the efficiency of the solar cell is calculated for different values of the absorber layer thickness *d* and for various internal quantum efficiency values $Q_i \in [10^{-6}; 1]$ (figure 4). The efficiencies were calculated using the materials' reflectivity R(E) as obtained from the first-principles calculations.
- Using this optimal thickness, we compute the maximal efficiency for a range of internal quantum efficiency values $Q_i \in [10^{-6}; 1]$ (figure 5). In addition, to highlight the impact of the absorber layer reflectivity on the solar cell properties, the calculation is performed with and without taking into account the materials' reflectivity R(E) in the calculation of the absorptance A(E) (equation (2)).
- Then, in figure 6, the current density voltage curves for the respective kesterite-based solar cells are presented for different internal quantum efficiency values $Q_i \in [10^{-6}; 1]$ and for a usual absorber layer thickness of 1.5 μ m.
- In table 3, the main solar cell electrical characteristics are reported first by assuming no non-radiative recombination (i.e. $Q_i = 1$) and secondly by assuming a non-radiative recombination rate fixed by $Q_i = 10^{-4}$ in order to obtain results comparable to actual experimental device characteristics (i.e. experimentally comparable V_{OC} values). Finally, the results obtained are compared to various experimental works.

In figure 4, the maximal efficiency is calculated as a function of the absorber layer thickness. Each curve represents an internal quantum efficiency value ranging logarithmically from 1 (highest efficiency) to 10^{-6}







the internal quantum efficiency $Q_i \in [10^{-6}; 1]$. Results from simulations taking into account the materials reflectivity R(E) are presented in full lines while dashed lines represent the maximal efficiencies obtained assuming R(E) = 0. In inset, evolution of the prefactor fixing the non-radiative recombination rate as described in equation (1) with respect of Q_i .

(lowest efficiency). Here, we report a significant disparity between the Cu₂ZnSiS₄-based solar cell efficiencies with values below 5% for all Q_i , compared to the cells based on the two other kesterite materials. This observation is linked to the larger bandgap of Cu₂ZnSiS₄, which limits drastically the short circuit current density (see supplementary material) as illustrated in figure 6 and table 3. The general trend observed for all materials is an increase of the efficiency as the absorber thickness increases over 10 nm. Then, for d just above 1 μ m, the efficiency reaches a plateau, for $Q_i = 1$, with maximal efficiency values of 25.71%, 19.85% and 3.1% respectively for the Sn-, Ge- and Si-kesterite compound. In contrast, for $Q_i < 1$, the efficiencies reach a maximal value for an optimal thickness before decaying linearly as d increases. The optimal thicknesses reported for the absorber layer thin films are between 1.15 and 2.68 μ m (cf. table 3). The observed increase of η with d can be explained by the optimisation of the absorptance function A(E) which gets closer to 1 - R(E)for $E > E_G$, thus maximising the short circuit current density. The optimisation of the absorptance also maximises $J_{rad,0}$ which reduces V_{OC} and reduces η but this phenomenon is not dominant here. Then, for a unit value of Q_i , J_{SC} asymptotically reaches a maximum value and any further increase of the thickness (over the optimal thickness value) does not result in any notable increase of the efficiency value. In contrast, for internal quantum efficiency values $Q_i < 1$, as the absorber layer gets thicker, the non-radiative recombination rate increases, leading to a decrease of the open circuit voltage and, consequently, to the efficiency drop (see supplementary material).

From the previous calculations, for each Q_i value, the absorber layer thickness giving the maximum efficiency is extracted as the optimal absorber thickness value d_{opt} . Then, in a second calculation (figure 5), the evolution of the maximal efficiency as a function of the internal quantum efficiency for an optimal thickness is reported both without (dashed lines, R(E) = 0) and with (full lines, R(E) from the DFT results in

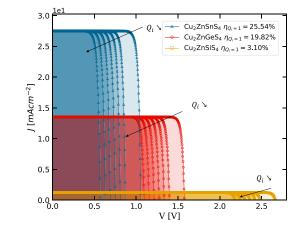


Figure 6. Current density-voltage curves of solar cell modelling for various internal quantum efficiency $Q_i \in [10^{-6}; 1]$. Results obtained for an absorber layer thickness of 1.5 μ m.

Table 3. Kesterite Cu_2ZnXS_4 (X = Sn, Ge, Si)-based solar cell efficiency modelling using the theoretical model proposed by Blank *et al* [36]. Short circuit current density J_{SC} , open circuit voltage V_{OC} , fill factor *FF* and cell efficiency η values are presented. For each calculation, the optimal absorber layer thickness d_{opt} has been precalculated and then used as parameter. Results are presented for an internal quantum efficiency $Q_i = 1$ and $Q_i = 10^{-4}$ for experimentally comparable V_{OC} values. In order to highlight the impact of the materials' reflectivity R(E), the calculation have been performed both for R(E) = 0 and for R(E) values as obtained using DFT calculations.

Materials	E_G (eV)	R(E)	Q_i	$d_{\rm opt} (\mu {\rm m})$	$J_{\rm SC}~({\rm mAcm}^{-2})$	$V_{\rm OC}$ (V)	FF [%]	η (%)	Exp.	Theo.
Cu ₂ ZnSnS ₄	1.32	0	1	2.68	35.69	1.06	88.62	33.38	[9]	[36, 59]
		0	10^{-4}	1.15	35.21	0.70	84.56	20.78		
		DFT	1	2.68	27.68	1.06	88.54	25.71		
		DFT	10^{-4}	1.15	27.19	0.70	84.39	15.88		
Cu ₂ ZnGeS ₄	1.89	0	1	2.02	17.62	1.58	91.65	25.95	[23]	[23, 30, 51]
		0	10^{-4}	1.15	17.53	1.23	89.82	19.65		
		DFT	1	2.02	13.55	1.58	91.59	19.85		
		DFT	10^{-4}	1.15	13.45	1.22	89.73	14.98		
Cu ₂ ZnSiS ₄	3.06	0	1	1.53	1.61	2.67	94.58	4.03	N.A.	N.A.
		0	10^{-4}	1.15	1.60	2.32	93.88	3.46		
		DFT	1	1.53	1.24	2.66	94.55	3.10		
		DFT	10^{-4}	1.15	1.23	2.31	93.85	2.66		

section 3.3) taking into account the materials' reflectivity in the absorptance calculation (see equation (2)). Concerning the impact of the materials' reflectivity on the solar cell efficiency for the Cu₂ZnSnS₄ compound, depending on the Q_i value, a percentage point loss of 4–8 in efficiency is observed (decrease of 4–6 observed for Cu₂ZnGeS₄ and of 1 for Cu₂ZnSiS₄). Concerning the behaviour of η with respect to Q_i , the cell efficiency increases as Q_i tends to unity and as the non-radiative recombination rate decays towards 0 (see equation (1)). Then, as the internal quantum efficiency decreases, the efficiencies reported also decrease with absolute percentage point losses of 1.54, 0.79 and 0.07 per order of magnitude, respectively for Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂ZnSiS₄. The variation of the slopes of the material curves observed in figure 5 from one kesterite to another is a direct consequence of the materials' optical property variations. Following the cationic substitution, the variation of the material absorptance function leads to a decrease of the radiative recombination rate value. As a consequence, for lower value of $R_{rad,0}$, a variation of Q_i implies a smaller variation of the non-radiative recombination rate and consequently of the total recombination rate. In addition, any increase of the saturation current density J_0 will lead to a decrease of the open circuit voltage and consequently of the efficiency. Combining these two explanations, as the material absorptance gets optimal with respect to the black body spectrum (i.e. from Cu₂ZnSiS₄ to Cu₂ZnSnS₄), the larger the radiative recombination rate is, the larger the efficiency variation per decade of Q_i will be (see supplementary material). Then, following the variation of the slope observed, for a fixed efficiency value (for example 15%), Cu_2ZnSnS_4 appears more 'robust' to larger non-radiative recombination rate as the Q_i value required to reach this efficiency is lower for Cu₂ZnSnS₄ than for Cu₂ZnGeS₄. This highlights the fact that even for a lower ratio of radiative over total recombination rates, a same efficiency is obtained. This tendency is reversed for Q_i values lower than 10^{-5} .

As shown in figure 6, the short circuit current density J_{SC} is independent of Q_i as this one is related to the total number of electron–hole pair generated by photons absorption (see supplementary material). This quantity depends only on the absorptance of the materials. Following the cationic substitution, the J_{SC} value decreases as the absorptance function worsen with respect to the solar spectrum. In opposition, an increase of the open circuit voltage is observed as the cation is substituted. Indeed, as the optical properties degrades, the radiative recombination rate decreases and consequently the V_{OC} value increases. In addition V_{OC} is Q_i dependent. For a given material, as Q_i tends towards a null value, the total recombination rate will increase resulting in a decrease of the V_{OC} value, leading to the decrease of the cell efficiency as reported in figure 5. Finally, the differences in η between the three kesterite materials are associated to the decreasing value of J_{SC} which is not fully compensated by the increase of the V_{OC} both attributed to the poorer absorptance as we move from the Sn-containing compound to the Si-containing compound.

In table 3, we report the electrical solar cell characteristics for each kesterite material incorporated as the absorber layer with the optimal thickness d_{opt} and for an internal quantum efficiency Q_i . Focusing on the results obtained using DFT-calculated reflectivity R(E) and using an internal quantum efficiency of $Q_i = 10^{-4}$ giving open circuit voltage value comparable to experimental ones [9], solar cell efficiencies of 15.88%, 14.98% and 2.66% are reported respectively for Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂ZnSiS₄ (for an optimal thickness of 1.15 μ m). In comparison to efficiency values obtained for vanishing radiative recombination rate (25.71%, 19.85% and 3.1% respectively for the Sn-, Ge- and Si-kesterite), one can observe a percentage point loss of nearly 10 for the Sn-compound (4.86 and 0.44 for the Ge- and Si-compound respectively). Then, experimentally, lower J_{SC} values around 21.5 mAcm⁻² and smaller fill factor values between 60% and 65% are reported [9]. This observation highlights that the predictions realised with this model corresponds to upper limits. Indeed, nor the materials' reflectivity or the absorption of the solar cell upper layers are taken into account, leading to an overestimation of J_{SC} . Concerning the fill factor, the electrical behaviour of the electrodes is assumed to be ideal. By repeating the calculation with a fixed short circuit current density matching the experimental value, a cell efficiency of 12.29% is reported as well as a V_{OC} value of 685 mV. This result is in good agreement with the values reported experimentally.

Using this methodology, we confirmed the interest regarding Cu_2ZnSnS_4 for the single-junction solar cell and we highlight a possible efficiency improvement of nearly 10% which might be achieved by reducing the non-radiative recombination rate. Then, Cu_2ZnGeS_4 might be interesting as the top cell for tandem approaches [23, 60] as this material provides higher bandgap value and interesting cell efficiencies, whereas, Cu_2ZnSiS_4 might be interesting for solar cell applications as PV windows.

4. Conclusion

In conclusion, we reported direct bandgap values of 1.32, 1.89 and 3.06 eV and absorption coefficients of the order of 10^4 cm⁻¹ for, respectively, Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂ZnSiS₄. Simultaneously a slight increase of the effective mass values is reported following the sequential substitution. Then, using as input data the optical properties of the materials, the solar cell electrical characteristics are predicted based on an improved version of the Shockley–Queisser model. Optimal absorber layer thicknesses between 1.15 and 2.68 μ m are reported and efficiencies of 25.71%, 19.85% and 3.10% are obtained for the kesterite compounds following the cationic substitution and the induced variation of the materials' properties. In addition, using optical results, we highlighted the negative impact of the materials' reflectivity on the solar cell characteristics. Using a non-radiative recombination rate giving V_{OC} values comparable to actual experimental measurements, we reported a decrease of the solar cell efficiencies to 15.88%, 14.98% and 2.66% respectively for Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂ZnSiS₄. Pointing out these results as upper limits, by reducing the non-radiative recombination current density, the efficiency of Cu₂ZnSnS₄ and Cu₂ZnGeS₄ could be improved respectively by 9.83% and 4.87%, putting forward these kesterite compounds as promising absorber layer materials.

Conflicts of interest

There are no conflicts to declare.

Data availability statement

The data that support the findings of this study are available upon reasonable request from the authors.

Acknowledgments

Computational resources have been provided by the Consortium des équipements de Calcul Intensif (CéCI), funded by the Fonds de la Recherche Scientifique de Belgique (F.R.S.-FNRS) under Grant No. 2.5020.11 and by the Walloon Region.

ORCID iDs

Thomas Ratz [©] https://orcid.org/0000-0002-3629-1087 Jean-Yves Raty [©] https://orcid.org/0000-0001-7535-2834 Guy Brammertz [®] https://orcid.org/0000-0003-1404-7339 Bart Vermang [©] https://orcid.org/0000-0003-2669-2087 Ngoc Duy Nguyen [©] https://orcid.org/0000-0002-0142-1611

References

- Vesborg P C K and Jaramillo T F 2012 Addressing the terawatt challenge: scalability in the supply of chemical elements for renewable energy RSC Adv. 2 7933
- [2] Communication from the Commission to the European Parliament, the Council, the European Economic and Social Committee and the Committee of the Regions on the 2017 list of Critical Raw Materials for the EU 2017 (accessed 19 November 2020)
- [3] Green M et al 2021 Solar cell efficiency tables (version 57) Prog. Photovolt., Res. Appl. 29 3
- [4] Nakamura M *et al* 2019 Cd-free Cu(In,Ga)(Se,S)₂ thin-film solar cell with record efficiency of 23.35% *IEEE J. Photovolt.* 9 1863
 [5] Giraldo S *et al* 2019 Progress and perspectives of thin film kesterite photovoltaic technology: a critical review *Adv. Mater.* 31 1806692
- [6] Wang W et al 2013 Device characteristics of CZTSSe thin-film solar cells with 12.6% efficiency Adv. Energy Mater. 4 1301465
- [7] Yan C et al 2018 Cu₂ZnSnS₄ solar cells with over 10% power conversion efficiency enabled by heterojunction heat treatment Nat. Energy 3 764
- [8] Todorov T et al 2020 Solution-based synthesis of kesterite thin film semiconductors J. Phys.: Energy 2 012003
- [9] Ratz T et al 2019 Physical routes for the synthesis of kesterite J. Phys.: Energy 1 042003
- [10] Grossberg M et al 2019 The electrical and optical properties of kesterites J. Phys.: Energy 1 044002
- [11] Platzer-Björkman C et al 2019 Back and front contacts in kesterite solar cells: state-of-the-art and open questions J. Phys.: Energy 1 044005
- [12] Crovetto A and Hansen O 2017 What is the band alignment of Cu₂ZnSn(S, Se)₄ solar cells ? Sol. Energy Mater. Sol. Cells 169 177
- [13] Chen S, Walsh A, Gong X-G and Wei S-H 2013 Classification of lattice defects in the kesterite Cu₂ZnSnS₄ and Cu₂ZnSnSe₄ earth-abundant solar cell absorbers Adv. Mater. 25 1522
- [14] Kim S, Park J-S and Walsh A 2018 Identification of killer defects in kesterite thin-film solar cells ACS Energy Lett. 3 496
- [15] Romanyuk Y E et al 2019 Doping and alloying of kesterites J. Phys.: Energy 1 044004
- [16] Li J, Wang D, Li X, Zeng Y and Zhang Y 2018 Cation substitution in Earth-abundant kesterite photovoltaic materials Adv. Sci. 5 1700744
- [17] Kumar M S, Madhusudanan S P and Batabyal S K 2018 Substitution of Zn in Earth-Abundant Cu₂ZnSn(S, Se)₄ based thin film solar cells–a status review Sol. Energy Mater. Sol. Cells 185 287
- [18] Tablero C 2014 Electronic and optical properties of substitutional V, Cr and Ir impurities in Cu₂ZnSnS₄ Sol. Energy Mater. Sol. Cells 125 8
- [19] Kim S, Kim K M, Tampo H, Shibata H and Niki S 2016 Improvement of voltage deficit of Ge-incorporated kesterite solar cell with 12.3% conversion efficiency Appl. Phys. Express 9 102301
- [20] Giraldo S et al 2018 How small amounts of Ge modify the formation pathways and crystallization of kesterites Energy Environ. Sci. 11 582
- [21] Buffière M et al 2015 Physical characterization of Cu₂ZnGeSe₄ thin films from annealing of Cu-Zn-Ge precursor layers Thin Solid Films 582 171
- [22] Choubrac L *et al* 2018 7.6% CZGSe solar cells thanks to optimized CdS chemical bath deposition *Phys. Status Solidi* a 215 1800043
 [23] Vermang B *et al* 2019 Wide band gap kesterite absorbers for thin film solar cells: potential and challenges for their deployment in
- tandem devices Sustain. Energy Fuels 3 2246
 [24] Khelifi S *et al* 2021 The path towards efficient wide band gap thin-film kesterite solar cells with transparent back contact for viable tandem application Sol. Energy Mater. Sol. Cells 219 110824
- [25] Chen S, *et al* 2010 Wurtzite-derived polytypes of kesterite and stannite quaternary chalcogenide semiconductors *Phys. Rev.* B 82 195203
- [26] Zamulko S, Chen R and Persson C 2017 Investigation of the structural, optical and electronic properties of Cu₂Zn(Sn,Si/Ge)(S/Se)₄ alloys for solar cell applications *Phys. Status Solidi* b 254 1700084
- [27] Liu H-R et al 2012 First-principles study on the effective masses of zinc-blend-derived Cu₂ZnIVVI₄ (IV=Sn, Ge, Si and VI=S, Se) J. Appl. Phys. 112 093717
- [28] Dun C, Holzwarth N, Li Y, Huang W and Carroll D L 2014 Cu₂ZnSn(S_xO_(1-x))₄ and Cu₂ZnSn(S_xSe_(1-x))₄: first principles simulations of optimal alloy configurations and their energies J. Appl. Phys. 115 193513
- [29] Walsh A, Chen S, Wei S-H and Gong X-G 2012 Kesterite thin-film solar cells: advances in materials modelling of Cu₂ZnSnS₄ Adv. Energy Mater. 2 400
- [30] Jiang J et al 2021 Inserting an intermediate band in Cu-and Ag-based Kesterite compounds by Sb doping: a first-principles study Mater. Sci. Eng. B 264 114937
- [31] Paier J, Asahi R, Nagoya A and Kresse G 2009 Cu_2ZnSnS_4 as a potential photovoltaic material: a hybrid Hartree-Fock density functional theory study *Phys. Rev. B* **79** 115126
- [32] Zhang Y et al 2012 Structural properties and quasiparticle band structures of Cu-based quaternary semiconductors for photovoltaic applications J. Appl. Phys. 111 063709

- [33] Gupta G K, Chaurasiya R and Dixit A 2019 Theoretical studies on structural, electronic and optical properties of kesterite and stannite Cu₂ZnGe(S/Se)₄ solar cell absorbers *Comput. Condens. Matter* **19** e00334
- [34] Shockley W and Queisser H J 1961 Detailed balance limit of efficiency of p-n junction solar cells J. Appl. Phys. 32 510
- [35] Heyd J, Scuseria G E and Ernzerhof M 2003 Hybrid functionals based on a screened Coulomb potential J. Chem. Phys. 118 8207
- [36] Blank B, Kirchartz T, Lany S and Rau U 2017 Selection metric for photovoltaic materials screening based on detailed-balance analysis Phys. Rev. Appl. 8 024032
- [37] Kresse G and Furthmüller J 1996 Efficiency of ab-initio total energy calculations for metals and semiconductors using a plane-wave basis set Comput. Mater. Sci. 6 15
- [38] Kresse G and Joubert D 1999 From ultrasoft pseudopotentials to the projector augmented-wave method Phys. Rev. B 59 1758
- [39] Perdew J P, Burke K and Ernzerhof M 1996 Generalized gradient approximation made simple Phys. Rev. Lett. 77 3865
- [40] Sun J, Ruzsinszky A and Perdew J P 2015 Strongly constrained and appropriately normed semilocal density functional *Phys. Rev. Lett.* 115 036402
- [41] Sun J et al 2016 Accurate first-principles structures and energies of diversely bonded systems from an efficient density functional Nat. Chem. 8 831
- [42] Fritsch D and Schorr S 2020 Climbing Jacob's ladder: a density functional theory case study for Ag₂ZnSnSe₄ and Cu₂ZnSnSe₄ J. Phys.: Energy 3 015002
- [43] Heyd J, Peralta J E, Scuseria G E and Martin R L 2005 Energy band gaps and lattice parameters evaluated with the Heyd-Scuseria-Ernzerhof screened hybrid functional J. Chem. Phys. 123 174101
- [44] Guo Q, Hillhouse H W and Agrawal R 2009 Synthesis of Cu₂ZnSnS₄ nanocrystal ink and its use for solar cells J. Am. Chem. Soc. 131 11672
- [45] Levcenko S, Tezlevan V, Arushanov E, Schorr S and Unold T 2012 Free-to-bound recombination in near stoichiometric Cu₂ZnSnS₄ single crystals *Phys. Rev. B* 86 045206
- [46] Lisunov K et al 2013 Features of the acceptor band and properties of localized carriers from studies of the variable-range hopping conduction in single crystals of p-Cu₂ZnSnS₄ Sol. Energy Mater. Sol. Cells 112 127
- [47] Chen J, Li W, Yan C, Huang S and Hao X 2015 Studies of compositional dependent Cu₂Zn(Ge_xSn_{1-x})S₄ thin films prepared by sulfurizing sputtered metallic precursors J. Alloys Compd. 621 154
- [48] Schorr S, Hoebler H-J and Tovar M 2007 A neutron diffraction study of the stannite-kesterite solid solution series Eur. J. Mineral. 19 65
- [49] Tsuji K, Maeda T and Wada T 2018 Optical properties and electronic structures of Cu₂ZnSnS₄, Cu₂ZnGeS₄ and Cu₂Zn(Ge,Sn)S₄ and Cu₂Zn(Ge,Sn)Se₄ solid solutions Japan. J. Appl. Phys. 57 08RC21
- [50] Khadka D B and Kim J 2013 Study of structural and optical properties of kesterite Cu₂ZnGeX₄ (X= S, Se) thin films synthesized by chemical spray pyrolysis CrystEngComm 15 10500
- [51] Courel M, Sanchez T, Mathews N and Mathew X 2018 Cu₂ZnGeS₄ thin films deposited by thermal evaporation: the impact of Ge concentration on physical properties J. Phys. D: Appl. Phys. 51 095107
- [52] Hamdi M et al 2014 Crystal chemistry and optical investigations of the Cu₂Zn(Sn,Si)S₄ series for photovoltaic applications J. Solid State Chem. 220 232
- [53] Levcenco S et al 2011 Polarization-dependent electrolyte electroreflectance study of Cu₂ZnSiS₄ and Cu₂ZnSiSe₄ single crystals J. Alloys Compd. 509 7105
- [54] Slater J C 1964 Atomic radii in crystals J. Chem. Phys. 41 3199
- [55] Heinrich C P, Day T W, Zeier W G, Snyder G J and Tremel W 2014 Effect of isovalent substitution on the thermoelectric properties of the Cu₂ZnGeSe_{4-x}S_x series of solid solutions J. Am. Chem. Soc. 136 442
- [56] Ikeda S *et al* 2019 Photocathode characteristics of a spray-deposited Cu₂ZnGeS₄ thin film for CO₂ reduction in a CO₂-saturated aqueous solution *ACS Appl. Energy Mater.* 2 6911
- [57] Garcia-Llamas E *et al* 2016 Wide band-gap tuning $Cu_2ZnSn_1 _xGe_xS_4$ single crystals: optical and vibrational properties *Sol. Energy Mater. Sol. Cells* 158 147
- [58] Vishwakarma M, Varandani D, Shivaprasad S and Mehta B 2018 Structural, optical, electrical properties and energy band diagram of Cu₂ZnSiS₄ thin films Sol. Energy Mater. Sol. Cells 174 577
- [59] Kim S, Márquez J A, Unold T and Walsh A 2020 Upper limit to the photovoltaic efficiency of imperfect crystals from first principles Energy Environ. Sci. 13 1481
- [60] El Radaf I and Al-Zahrani H 2020 Facile synthesis and structural, linear and nonlinear optical investigation of p-type Cu₂ZnGeS₄ thin films as a potential absorber layer for solar cells J. Electron. Mater. 49 4843